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# Kinetic analysis of anaerobic sequencing batch reactor for the treatment of tannery wastewater 

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#### Abstract

A pilot scale anaerobic sequencing batch reactor (ASBR) was operated at different organic loading rate  and methane production kinetic models. The system was operated at mesophilic temperature. The wastewater was fed using submersible pump in every twenty four hours and agitated with hydraulic pump for fifteen minutes in every one hour. The COD removal efficiencies was found to be between 69$85 \%$ and the methane yield was also between $0.17 \pm 0.2$ and $0.30 \pm 0.02 \mathrm{~m}^{3} / \mathrm{kg}$ COD removed. In the kinetic studies, modified Stover-Kincannon and second-order models were found to be the most appropriate model for ASBR treating tannery wastewater than first order model. The saturation value constant and maximum COD removal rate found in Stover-Kincannon model were 5.57 and 5.56 kg of COD m${ }^{-3} . \mathrm{d}^{-1}$, respectively. The kinetic studies of volumetric methane production showed that Michaelis-Menten model was found to be capable of predicting the volumetric methane production in ASBR that treat tanney wastewater.


Key words: Anaerobic sequencing batch reactor (ASBR), chemical oxygen demand (COD) removal, MichaelisMenten, second order, Stover-Kincannon.

## INTRODUCTION

Tanning is almost a wet process that uses about 30 to 40 L of water/kg of hides or skin processed and also discharges about $90 \%$ of the consumed water as wastewater (IFC, 2007). The wastewaters, which are discharged without proper treatment, would contaminate surface and ground water as well as soils. A tanning industry can cause groundwater pollution of about 7 to 8 km radius (Mondal et al., 2005). Currently, there are more
than 30 tanneries under operation in Ethiopia. These tanning industries generate $11,312 \mathrm{~m}^{3}$ wastewater per day and disposed to the surrounding water bodies without proper treatments (LIDI, 2010). However, it is characterized by a high load of pollutants which require proper treatment before it would be discharged into the receiving water body. The treatment systems adopted by most industries are frequently considered as

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Figure 1. Schematic diagram of the pilot scale anaerobic sequencing batch reactor. ASBR (1); control panel (2); mixing chamber (3); feeding pipe (4); gas pipe (5); gas flow meter (6); moisture trap unit (7); biogas storage bag (8): gas valve (9); gas blower (10); sulfur scrubber (11); generator (12) and gas line to the kitchen (13).
regulatory obligation that increase capital and operational costs and ultimately yield negative economic returns. Compliance to environmental legislations should not necessary lead to the creation of additional costs. It should instead provide a secondary source of income. Anaerobic treatment is considered as sustainable method of reducing pollution from domestic, agricultural and industrial operations (Seghezzo et al., 1998; William and David, 1999). It consumes little energy as no aeration is needed and produces renewable energy in the form of biogas and nutrient rich digestate (Kaparaju and Rintala, 2011). Beside the supply of energy and manure, the anaerobic technology provides the opportunity for the reduction of greenhouse gas emission and mitigation of global warming through substitution of fossil fuel for energy production and chemical fertilizer (Pathak et al., 2009). The total output in $\mathrm{CO}_{2}$ equivalents might be reduced from $2.4 \mathrm{~kg} \mathrm{CO}_{2}$-eq/kg COD removed for fully aerobic treatment to 1.0 kg for primarily anaerobic processes (Insam and Wett, 2008). In fully aerobic system, up to $1.4 \mathrm{~kg} \mathrm{CO}_{2} / \mathrm{COD}$ removed is generated from electric power generation, whereas the carbon dioxide generated in the anaerobic processes is greenhouse gas neutral (Insam and Wett, 2008; Kaparaju and Rintala, 2011).

The anaerobic sequencing batch reactor (ASBR) operates in a cyclic batch mode with four distinct phases per cycle. The four phases are: filling, reacting, settling and release (Timur and Oèzturkm, 1999; Zhang et al., 1997). The ASBR systems has been successfully applied in laboratory and pilot scales for treatment of high strength wastewaters including landfill leachate,
slaughterhouse wastewater, municipal sludge and dairy wastewaters, and brewery wastewater (Xiangwen et al., 2008).

Mathematical description of biological treatment processes has been performed using process kinetics model. The understanding of process kinetics is important for the design of specific unit and operation of treatment systems, predicting system stability, effluent quality and waste stabilization. The knowledge on kinetics model leads to optimization of performance, a more stable operation and a better control of wastewater treatment operations. There are numerous mathematical models in the literature for describing anaerobic processes such as first order model, second-order, Grau model, Modified Stover-Kincannon, Sundstorm model, Contois model, Chen, Michaelis-Menten type kinetic model, etc (Jafarzadeh et al., 2009; Sandhya and Swaminathan, 2006; Buyukkamaci and Filibeli, 2002). In this study, different mathematical models such as first order model, second order Grau model, Modified StoverKincannon, Michaelis-Menten type kinetic model were applied to data obtained from the ASBR operation and kinetic coefficient for the reactors were calculated.

## MATERIALS AND METHODS

## Experimental set up

The pilot-scale anaerobic SBR was constructed using concrete materials in a cylindrical in shape with a dimension of 4 m in height and 4 m in diameter. Figure 1 shows the schematic diagram of the pilot scale ASBR and the accessories. The total volume was $100 \mathrm{~m}^{3}$

Table 1. Characteristics of tannery wastewater used at five different OLR.

| Parameter | Phase I | Phase II | Phase III | Phase IV |
| :--- | :---: | :---: | :---: | :---: |
| pH | $9.64 \pm 0.46$ | $9.20 \pm 0.33$ | $9.28 \pm 0.311$ | $9.09 \pm 0.49$ |
| E.C. $(\mathrm{mS})$ | $8.76 \pm 0.40$ | $8.46 \pm 0.39$ | $8.08 \pm 0.38$ | $8.43 \pm 0.72$ |
| TDS $(\mathrm{g} / \mathrm{l})$ | $7.49 \pm 0.36$ | $7.24 \pm 0.44$ | $6.81 \pm 0.42$ | $7.26 \pm 0.68$ |
| Salinity $(\mathrm{g} / \mathrm{l})$ | $9.26 \pm 0.57$ | $9.19 \pm 0.38$ | $8.91 \pm 0.33$ | $9.07 \pm 0.71$ |
| $\mathrm{COD}(\mathrm{mg} / \mathrm{l})$ | $4221 \pm 359$ | $4265 \pm 215$ | $4586 \pm 292$ | $4458 \pm 396$ |
| $\mathrm{TN}(\mathrm{mg} / \mathrm{l})$ | $451 \pm 47.5$ | $517 \pm 112$ | $492.5 \pm 89.9$ | $458 \pm 58.6$ |
| $\mathrm{NH}_{4}{ }^{+}-\mathrm{N}(\mathrm{mg} / \mathrm{l})$ | $231 \pm 45$ | $270 \pm 66$ | $255 \pm 58$ | $248 \pm 44.46$ |
| Total phosphorus $(\mathrm{mg} / \mathrm{l})^{22.2 \pm 6.8}$ | $18 \pm 4.5$ | $19.3 \pm 4.16$ | $23.5 \pm 6.5$ |  |
| Sulfide $(\mathrm{mg} / \mathrm{l})$ | $93 \pm 22.27$ | $126 \pm 38.9$ | $123.5 \pm 33.8$ | $117.5 \pm 29.4$ |
| Sulfate $(\mathrm{mg} / \mathrm{l})$ | $470 \pm 75$. | $390 \pm 76.9$ | $520 \pm 99.13$ | $469 \pm 69$ |

of this $80 \mathrm{~m}^{3}$ as working volume and the remaining volume for head space. The internal part of the digester was insulated with plastic foam and covered with geo-membrane. Stainless steel tubes were installed 30 cm above the bottom of the digester surface for the circulation of hot water. The top of the digester has two holes. One of the holes was fitted with PVC pipe for biogas outlet to gas flow meter and to the gas storage bag. The other one was fitted with stainless steel tubing extended to the bottom of the digester for hot water circulation. The ASBR was operated under mesophilic condition $\left(31^{\circ} \mathrm{C}\right)$ and hot water heated with solar panel was used to maintain the temperature. The wastewater in the ASBR was mixed in every hour using hydraulic pump for fifteen minutes during the day time of the operation.

## Operation of the ASBR

The performance of the pilot scale ASBR was evaluated at four different OLRs. The performance of the ASBR was monitored by measuring COD removal efficiency and the biogas production and quality. During the first phase, the reactor was operated at the organic loading rate (OLR) of $1.03 \mathrm{~kg} \cdot \mathrm{~m}^{-3} \cdot \mathrm{~d}^{-1}$ and constant hydraulic retention time of 4 days. In the second phase, the OLR was increased from 1.03 to $1.23 \mathrm{~kg} \cdot \mathrm{~m}^{-3} . \mathrm{d}^{-1}$ by increasing the volume of wastewater from 20 to $23 \mathrm{~m}^{3}$ and HRT was 3.5 days. In the third phase, the reactor was operated at OLR of $1.52 \mathrm{~kg} \cdot \mathrm{~m}^{-3} \cdot \mathrm{~d}^{-1}$ and HRT of 3 days by increasing the volume of the inlet wastewater from 23 to $26.5 \mathrm{~m}^{3}$. Finally, it was operated at OLR of $2.21 \mathrm{~kg} \cdot \mathrm{~m}^{-3} . \mathrm{d}^{-1}$ and 2 days by increasing the volume of wastewater from 26.5 and $40 \mathrm{~m}^{3}$.

## Physico-chemical analysis

The characteristics of influent and effluents were determined in terms of chemical oxygen demand (COD), total nitrogen (TN), ammonium-nitrogen $\left(\mathrm{NH}_{4}{ }^{+}-\mathrm{N}\right)$, nitrate-nitrogen $\left(\mathrm{NO}_{3}-\mathrm{N}\right)$, sulphides ( $\mathrm{S}^{2-}$ ), sulphate $\left(\mathrm{SO}_{4}{ }^{2-}\right.$ ), total phosphorous (TP) and orthophosphate ( $\mathrm{PO}_{4}{ }^{3-}$ ) colorimetrically using spectrophotometer (DR/2010 HACH, Loveland, USA) according to HACH instructions. Total solid and volatile solid were also measured according to the methods described in standard methods of water and wastewater (APHA, 1998). pH of tannery wastewater was measured using a pH meter (CON, 2700). TDS, EC and salinity were measured using TDS/EC/salinity meter. Sodium, potassium, calcium, magnesium, chromium, copper, iron and lead were determined using an atomic absorption spectrometer (novAA, 400P). Total nitrogen content of
the wetland plant samples was determined by Kjeldahl method. Percent of removal efficiency (\%) for each parameter was determined by the following equation:
$\operatorname{RE}(\%)=100 *\left(\frac{S_{\text {In }-} S_{\text {out }}}{S_{\text {In }}}\right)$

## RESULTS AND DISCUSSION

## Characteristics of raw tannery wastewater

Tannery wastewater is characterized mostly in terms of the levels of pH , salinity, organic matter (COD), nitrogenous compounds (TN and $\mathrm{NH}_{4}{ }^{+}$), suspended solids (SS) and total dissolved solids (TDS), chromium and sulfides (Jahan et al., 2014). However, these parameters vary significantly from tannery to tannery depending on the size of the tannery, chemicals used for a specific process, amount of water used and type of final product produced.

The mean characteristics of raw wastewaters used in the study are presented in Table 1.

The wastewater was characterized as alkaline with pH value ranging from $9.09 \pm 0.49$ to $9.64 \pm 0.46$. It also contain high level of electrical conductivity $(8.08 \pm 0.38$ to $8.76 \pm 0.34 \mathrm{mS})$, total dissolved solids $(6.81 \pm 0.42$ to $7.49 \pm 0.36 \mathrm{~g} / \mathrm{l})$ and salinity content $(8.77 \pm 0.72$ to $9.26 \pm 0.51 \mathrm{~g} / \mathrm{l})$. This due to the chemicals used in the soaking and beam house operation. It contained high organic matter and nitrogenous compounds with COD ranges from $4221 \pm 359$ to $4586 \pm 292 \mathrm{mg} / \mathrm{l}$. The influent had high total nitrogen (TN), $\mathrm{NH}_{4}{ }^{+}-\mathrm{N}$ and sulfate values ranges from $451 \pm 47.5$ to $517 \pm 112 \mathrm{mg} / \mathrm{l}, 231 \pm 45$ to $270 \pm 66 \mathrm{mg} / \mathrm{l}$ and $390 \pm 76.9$ to $520 \pm 99.13 \mathrm{mg} / \mathrm{l}$, respectively; likewise, sulfide and phosphate concentrations ranged from $92.9 \pm 23.27$ to $127 \pm 43.3 \mathrm{mg} / \mathrm{l}$ and $18 \pm 4.5$ to $23.5 \pm 6.5 \mathrm{mg} / \mathrm{l}$, respectively. Seyoum (2004) reported higher concentration of TN, ammonium and COD in tannery wastewater.

Table 2. Summary of the performance of anaerobic sequencing batch reactor.

| Parameters | Phase I | Phase II | Phase III | Phase IV |
| :--- | :---: | :---: | :---: | :---: |
| OLR $\left(\mathrm{kg} \cdot \mathrm{m}^{-3} \cdot \mathrm{day}^{-1}\right)$ | $1.03 \pm 0.09$ | $1.23 \pm 0.06$ | $1.52 \pm 0.1$ | $2.21 \pm 0.23$ |
| HRT (day) | 4 | 3.5 | 3 | 2 |
| COD removal $(\%)$ | $81 \pm 2.1$ | $79 \pm 2.3$ | $76 \pm 1.6$ | $69 \pm 1.7$ |
| COD out $(\mathrm{mg} / \mathrm{l})$ | $791 \pm 149.5$ | $898.9 \pm 122$ | $1101.4 \pm 123$ | $1358.3 \pm 170$ |
| Biogas production $\left(\mathrm{m}^{3} . \mathrm{day}^{-1}\right)$ | $26.2 \pm 1.6$ | $28.1 \pm 1.8$ | $31.8 \pm 2.7$ | $36.7 \pm 2.8$ |
| Methane $(\%)$ | $70 \pm 1.6$ | $68 \pm 1.7$ | $64 \pm 3.0$ | $55 \pm 1.9$ |

## Performance of the ASBR

The COD removal efficiency and biogas production, methane yield and content of the ASBR are summarized in Table 2. During the first phase of the operation, the COD removal efficiency varied in the range of $78-84 \%$. The average COD removal efficiency and mass removal rate in the single feeding mode were $81 \pm 2 \%$ and $791 \pm 149.5 \mathrm{mg} / \mathrm{l}$, respectively.
In the second phase, the COD removal efficiency varied in the range of 76 to $83 \%$ with average removal efficiency of $79 \pm 2.3 \%$, while the average concentration of COD was $898.9 \pm 122 \mathrm{mg} / \mathrm{l}$ in the final effluent. In the third phase, the average COD removal efficiency decreased to $74-79 \%$ with average COD concentration of $1101.4 \pm 123$ $\mathrm{mg} / \mathrm{l}$. In the final phase, the COD removal efficiency varied between 67 and $72 \%$. The average removal COD removal efficiency and effluent concentration were $69 \pm 1.7 \%$ with $1358.3 \pm 170 \mathrm{mg} / \mathrm{l}$, respectively. The anaerobic digester showed significant variation in COD removal efficiency with variation of organic loading rate (ANOVA, $\mathrm{P}<0.05$ ). The results of this study indicate that COD removal efficiency was highest in the first phase of operation and lowest in the final phase of operation. The final phase showed residual COD $31 \%$ from the influent. The COD removal efficiencies obtained in this study were higher than the results recorded by Song et al. (2003) from the treatment of tannery wastewater (COD removal of 60 to $75 \%$ ) using upflow anaerobic fixed biofilm reactor at varying organic loading rate of 0.16 to $3.14 \mathrm{~kg} \mathrm{~m}^{-3} \mathrm{~d}^{-1}$ and HRT of 16 days to 1 day. The results obtained in phase II $(79 \pm 2.3 \%)$ are comparable with results reported by Lefebvre et al. (2006) for the treatment of tannery soak liquor (COD removal of $78 \%$ ) at a HRT of 5 days and an OLR of $0.5 \mathrm{~kg} \mathrm{~m}^{-3} \mathrm{~d}^{-1}$ using up flow anaerobic sludge blanket bed reactor. Other comparable mean COD removal (78.2\%) was reported by El-Sheikh et al. (2011) in the treatment of tannery wastewater using two stage UASB reactors. On the other hand, Banu and Kaliappan (2007) found slightly higher COD removal efficiency ( $86 \%$ at OLR of $2.74 \mathrm{~kg} \mathrm{~m}^{-3} \mathrm{~d}^{-1}$ and HRT of 60 h ; $88 \%$ at OLR of $3.22 \mathrm{~kg} \mathrm{~m}^{-3} \mathrm{~d}^{-1}$ for 70 h ) in the treatment of tannery wastewater using hybrid upflow anaerobic sludge blanket reactor.

## Kinetic model substrate removal

## First order substrate removal model

The hydrolysis of organic pollutants was described by first order kinetics model. The mass balance equation for the substrate in the anaerobic system can be described as follows:
$-\frac{\mathrm{ds}}{\mathrm{dt}}=\frac{\mathrm{Q}}{\mathrm{V}}\left(\mathrm{S}_{o-} \mathrm{S}_{\mathrm{e}}\right)-K 1 S e$
where, So is substrate concentration in the influent ( $\mathrm{mg} / \mathrm{l}$ ): Se is substrate concentration in the effluent; Q is flow rate of influent to reactor (l/d); V is effective volume of the reactor and K1 is first-order kinetic constant (per day). Under steady state conditions, $\left(-\frac{\mathrm{ds}}{\mathrm{dt}}\right)=0$ and the above equation can be represented in the following form:
$\frac{\mathrm{S}_{0-} S e}{\theta_{\mathrm{H}}}=K 1 S e$
where, $\theta_{\mathrm{H}}=$ hydraulic retention time .
The value of first-order kinetic constant can be obtained by plotting $\frac{\mathrm{S}_{0}-\mathrm{Se}}{\theta_{\mathrm{H}}}$ against Se as given in the above equation. The slope of the line in the plot would represent the value of $\mathrm{K}_{1}$. The first order model for COD removal is drawn in Figure 2. The value of the k was obtained from the slope of the line that was plotted ( $\mathrm{So}-\mathrm{Se}$ )/HRT versus Se . The graph fit a straight line with regression coefficient of ( $R^{2}=0.83$ ).
This indicates that about $17 \%$ of the total variations were not explained in the first order regression model. The k value was determined as 0.99 per day. Isik and Sponza (2005) obtained comparable ( $\mathrm{k}=0.93$ ) value with this study from the treatment simulated textile wastewater using UASBR system

## Modified Stover-Kincannon Model

The Stover-Kincannon was developed first for rotating biofilm reactor (Sandhye and Swaminathan, 2006). It is


Figure 2. Substrate removal first order model for ASBR.
assumed that the organic loading rate can be correlated with substrate utilization rate using mono-molecular kinetics. The substrate removal rate is defined in two different forms as shown below:
$\frac{\mathrm{ds}}{\mathrm{dt}}=\frac{\mathrm{Q}}{\mathrm{V}}\left(\mathrm{S}_{\left.\mathrm{i}_{-} \mathrm{S}_{\mathrm{e}}\right)}\right)$
$\frac{\mathrm{ds}}{\mathrm{dt}}=\frac{\mathrm{U}_{\text {max }}\left(\frac{\mathrm{QS}_{i}}{\mathrm{~V}}\right)}{\mathrm{K}_{\mathrm{B}}+\left(\frac{\mathrm{QS} S_{i}}{\mathrm{~V}}\right)}$
This can be linearized as:

$$
\left(\frac{d s}{d t}\right)^{-1}=\frac{V}{q(S i-S e)}=\frac{K B V}{U \max Q S i}+\frac{1}{U \max }
$$

Where ds/dt is the substrate removal rate ( $\mathrm{g} / \mathrm{L}$-day), $\mathrm{U}_{\text {max }}$ is the maximum utilization rate constant ( $\mathrm{g} / \mathrm{L}$-day), $\mathrm{K}_{\mathrm{B}}$ is saturation value constant ( $\mathrm{g} / \mathrm{L}$-day), Q is the flow rate (L/day) and V is the effective volume of reactor (L). Since $\mathrm{dS} / \mathrm{dt}$ approaches $\mathrm{U}_{\text {max }}$ as the organic loading rate, qSi/V approaches infinity. Figure 3 illustrates the graph drawn between the reciprocal of mass loading removal rate ( $\mathrm{V} /(\mathrm{Q}(\mathrm{So}-\mathrm{Si})$ with the reciprocal of OLR to derive the values of Umax and $K_{B}$ for the anaerobic sequencing batch reactor treating tannery wastewater. The graph fit a straight line with regression coefficient of $\left(R^{2}=0.99\right)$. This indicates that only less than $1 \%$ of the total variations were not explained in the regression model. Hence, the
regression coefficient supports strongly the validity of the linearized Stover-Kincannon model. It can be conclude that modified Stover-Kincannon model can be used to describe the performance of mesophilic ASBR treating tannery wastewater in this study. The maximum value for COD removal rate ( $\mathrm{U}_{\text {max }}$ ) and saturation constant ( $\mathrm{K}_{\mathrm{B}}$ ) were determined as 5.56 and 5.78 kg of COD m${ }^{-3} \mathrm{~d}^{-1}$, respectively.
The predicted $U_{\text {max }}$ was higher than the maximum loading rate ( $2.21 \mathrm{~kg} \mathrm{~m}^{-3} \mathrm{~d}^{-1}$ ) used in this study. This revealed that ASBR has higher potential in withstanding high strength tannery wastewater. Moreover, the closeness of $U_{\text {max }}$ and $\mathrm{K}_{B}$ values obtained indicate that increasing organic loading rates would lead to reduction in the processes efficiency. Senturk et al. (2010) and Ahn and Forster (2000) also made similar conclusion. Table 3 shows the comparison of the value of $\mathrm{U}_{\text {max }}$ and $\mathrm{K}_{\mathrm{B}}$ reported for various types of substrate (wastewater) using the same type of modified Stover-Kincannon model.
The $\mathrm{U}_{\text {max }}$ and $\mathrm{K}_{\mathrm{B}}$ found in this current work were higher than Priya et al. (2009) and Ahn and Forster (2002). They were almost comparable with the values obtained by Kapdan (2005) and Isik and Sponza (2005). On the other hand, the value of both Umax and $\mathrm{K}_{\mathrm{B}}$ in this work were lower than that of Senturk et al. (2010), Wanga et al. (2009), Yilmaz et al. (2008) and Sandhye and Swaminathan (2006). The highest $U_{\text {max }}$ were obtained for milk permeate waste water in AMBBR system followed by paper mill wastewater, while the lowest was for formaldhyde containing wastewater followed by corrugated paper wastewater. On the other hand, the


Figure 3. Modified Stover-Kincannon model for ASBR.

Table 3. Comparison of the kinetic parameters obtained for the various substrates.

| Types of wastewater | Reactor | $\mathbf{U}_{\max }$ | $\mathbf{K}_{\mathbf{B}}$ | References |
| :--- | :--- | :--- | :--- | :--- |
| Tannery | ASBR | 5.56 | 5.78 | This study |
| Food processing wastewater | Anaerobic contact | 22.92 | 23.59 | Senturk et al. (2010) |
| Formaldhyde containing wastewater | UAFB | 3.4 | 4.6 | Priya et al. (2009) |
| Milk permeate wastewater | AMBBR | 89.3 | 102.3 | Wanga et al. (2009) |
| Paper mill wastewater | AF | 86.21 | 104.15 | Yilmaz et al.(2008) |
| Textile wastewater | UAFB | 31.69 | 45.37 | Sandhye and Swaminathan (2006) |
| Simulated Textile wastewater | UASBR | 7.5 | 8.2 | Isik and Sponza (2005) |
| Synthetic saline wastewater | UASBR | 5.3 | 7.05 | Kapdan (2005) |
| Corrugated paper wastewater | AF | 3.86 | 0.80 | Ahn and Forster (2002) |

highest $K_{B}$ was found for paper mill wastewater followed by milk permeates wastewater, while the lowest was from corrugated paper wastewater. The variation of $U_{\max }$ and $K_{B}$ values among different researchers might be attributed to the variation of characteristics wastewater, reactor configuration and microorganisms used in the studies (Priya et al., 2009).

## Grau second-order model

The second order model was employed to the experimental results for ASBR system treating tannery
wastewater. The general equation of Grau second order kinetics model is shown below:
$\frac{\mathrm{ds}}{\mathrm{dt}}=\mathrm{k}_{2} \mathrm{X}\left(\frac{\mathrm{s}}{\mathrm{s}_{\mathrm{o}}}\right)^{2}$
Where, $d s / d t$ is the substrate removal rate ( $g / L$-day), $k_{2}$ is kinetic constant ( g COD/gVS-day), X is the concentration of microorganisms ( $\mathrm{gVS} / \mathrm{L}$ ), S is substrate concentration at any time, and $S_{0}$ is the concentration of initial substrate ( $\mathrm{g} / \mathrm{l}$ ).

Integrating the above equation within the boundary conditions ( $\mathrm{S}=\mathrm{Si}$ to Se and $\mathrm{t}=0 \mathrm{to} \theta_{\mathrm{H}}$ ), and then linearized,


Figure 4. Linear plots of the Grau second-order kinetic model.
the following equation is obtained.
$\frac{\mathrm{S}_{0} \theta_{\mathrm{H}}}{\mathrm{S}_{0}-\mathrm{S}}=\theta_{\mathrm{H}}+\frac{\mathrm{S}_{0}}{\mathrm{k}_{2} \mathrm{X}}$
Holding the term " $\mathrm{S}_{0} / \mathrm{k}_{2} \mathrm{X}$ " in the above equation constant leads to
$\frac{\mathrm{S}_{0} \theta_{\mathrm{H}}}{\mathrm{S}_{0}-\mathrm{S}}=a+b \theta_{\mathrm{H}}$
The term $\left(\mathrm{S}_{0}-\mathrm{S}_{\mathrm{i}}\right) / \mathrm{S}_{0}$ is the substrate removal efficiency (E) and it can be used in the equation as shown below:
$\frac{\theta_{\mathrm{H}}}{E}=a+b \theta_{\mathrm{H}}$
If $\mathrm{V} / \mathrm{Q}(\mathrm{Si}-\mathrm{Se})$ is plotted against $1 / \mathrm{OLR}, \mathrm{K}_{\mathrm{B}} / \mathrm{U}_{\text {max }}$ is the slope and $1 / \bigcup_{\max }$ is the intercept point of the line. Figure 4 shows the plot of the Grau second-order multicomponent model for ASBR.

The value of $a$, and $b$ were determined from the intercept and slope of the straight lines. The values of a and $b$ were obtained to be 0.87 and 1.019 , respectively, with high correlation coefficient ( $\mathrm{R}^{2}=0.99$ ). This confirms the validity of the application of this model for ASBR treating tannery wastewater. Hence, the formula for predicting substrate concentration in the effluent can be given as:
$S=S_{0}\left(1-\frac{\theta}{0.87+1.019 \theta}\right)$

These results show that both modified Stover-Kincannon model and Grau second-order can be applied successfully for modeling of the experimental results of ASBR treating tannery wastewater with high correlation coefficient ( $R^{2}=0.99$ ). On the other hand, the first order model appeared to be less successful $\left(R^{2}=0.83\right)$ on predicting substrate removal from tannery wastewater in ASBR system.

## Kinetics of methane production

The volumetric methane production rate can be obtained through the expression:
$r_{C H_{4}}=\frac{q_{C H_{4}}}{V}$
where $\mathrm{qCH}_{4}$ is the daily methane production ( $\mathrm{m}^{3} / \mathrm{d}$ ) and V is the reactor working volume $\left(\mathrm{m}^{3}\right)$.

Figure 5 illustrate the graphical estimation of the concentration of non-biodegradable organic matter (TCOD) based on the relationship between In (TCOD) and $1 /(\mathrm{HRT})$ (Wang et al., 2009). By the least-square fitting of In (TCOD) and 1/HRT, an intercept of 0.531 g TCOD $L^{-1}$ (regression coefficient 0.95 ) was calculated, which corresponds to an infinite HRT. Thus, this can be considered to be the amount of non-biodegradable substrate (Borja et al., 2003; Raposo et al., 2004; Rincon et al., 2006; Wang et al., 2009).
Senturk et al. (2010) and Rincon et al. (2006) found


Figure 5. Estimation of the fraction of non-biodegradable soluble organic matter contained in the wastewater used in the study.

Figure 6. Variation of the volumetric methane production rates $\left(\boldsymbol{r}_{\mathrm{CH}_{4}}\right)$ as a function of the biodegradable TCOD concentration.
lower non-biodegradable substrate (290 and $92 \mathrm{mg} / \mathrm{l}$ ) in reactors treating wastewater generated from food processing and protein production from chickpea, respectively. On the other hand, Borja et al. (2003) and Wang et al. (2009) determined higher valu

es of non-biodegradable substrate in the treatment of wastewater generated from Olive Pomace and diary industry, respectively.
The observed values of $\quad r_{\mathrm{CH}_{4}}$ (methane production) plotted as a function of biodegrdabel organic matter concentration (TCOD biod) are shown in Figure 6. As shown in the figure, the observed methane production


Figure 7. Comparsion between the experimental methane proudction rates and the theoretical value predicted.
values fit Michaelis-Menten type kinetic model, which is a hyperbolic function. By using the origin 8 software, the following kinetic equation was obtained:
$r_{C H_{4}}=0.281 T C O D b /(T C O D b+0.112)$
The theortical $r_{\text {CH }_{4}}$ values could be determined using the above equation for the reactor used in this study. The predicted thoertical methane production values were plotted against the observed methane production values. As shown in Figure 7, a linear regression line with a slope of 1.01 and a regression coefficient of the graph 0.99 were obtained. This indicted that the proposed model is capable of predicting the behavior of the ASBR treating tanney wastewater.

## Conclusion

The results of this study showed that tannery wastewater could be treated efficiently in anaerobic sequencing batch reactor at different HRT (4, 3.5, 3 and 2 days). The tannery wastewater treatment performance of the ASBR was evaluated at different organic loading rate of 1.03, $1.23,1.52$ and $2.21 \mathrm{~kg} \mathrm{~m}^{-3} \cdot \mathrm{~d}^{-1}$ and the kinetic analysis for the reactor was performed using the data found in the experiment. The results of the system showed that COD
removal efficiency was 69 to $85 \%$ and the methane yield was $0.17 \pm 0.2$ to $0.30 \pm 0.02 \mathrm{~m}^{3} / \mathrm{kg}$ COD removed. Modified Stover-Kincannon and second-order models were found to be the most suitable model for ASBR ( $\mathrm{R}^{2}=$ 0.99 ). Michaelis-Menten model was also found to be capable of predicting the volumetric methane production of ASBR that treat tanney wastewater.

## CONFLICT OF INTERESTS

The authors have not declared any conflict of interests.

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